

MATHEMATICAL MODELS FOR BIOMEDICAL AND BIOLOGICAL SYSTEMS
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Electrophysiology of nerve and heart muscle

- **Passive (RC) properties of a nerve fiber:** Hodgkin, A.L., and Rushton, W.A.H. "The Electrical Constants of a Crustacean Nerve Fibre." *Proc. Royal Soc. B*, 133:444-479, 1946.
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